INTRODUCTION

Conventionally, possible ground states of a disordered two-dimensional (2D) electron system at zero temperature include superconducting, quantum Hall liquid, or insulating phases. However, transport studies near the magnetic field–tuned superconductor-insulator transition in strongly disordered films suggested the emergence of anomalous metallic phases that persist in the zero-temperature limit, with resistances ($\rho_{xx}$) much lower than their respective nonsuperconducting state values ($\rho_{ss}$) (extrapolated from above the superconduction transition temperature $T_c$). Initial studies of these phases on amorphous MoGe films (1–3) were followed by similar observations in amorphous indium oxide (4, 5), tantalum (6), and indium-gold alloy (7) films, as well as in crystalline materials (8, 9) and hybrid systems consisting of a superconducting metal in contact with a 2D electron gas, such as tin-graphene (10). Metallic phases were also observed in weakly disordered 2D superconductors at zero field when either disorder or carrier density is tuned (10–13).

Despite the ubiquitous appearance of this metallic phase, progress in understanding its origin has been slow. Early theoretical treatments explored quantum fluctuations in the presence of a dissipative bath, presumably due to residual fermionic excitations (14–18), a Bose metal phase (19, 20), and an exotic non–Fermi liquid vortex metal phase (21, 22). Finally, noting that the distribution of the superconducting order parameter is highly inhomogeneous in the presence of disorder, Spivak et al. (23) examined a metallic phase that is stabilized by quantum fluctuations while showing significant superconducting correlations. To date, there has been no conclusive evidence that distinguishes any one of these scenarios.

Here, we present evidence that the anomalous metallic phase can be described as a "failed superconductor," where particle-hole symmetry, reminiscent of the superconducting state, plays a major role in determining its properties. This conclusion is a result of extensive Hall effect measurements on amorphous tantalum nitride (TaN$_x$) and indium oxide (InO$_x$) films that are weakly disordered (24). Specifically, we find that $\rho_{xx}$ in both systems becomes finite at the transition from a "true superconductor" to an anomalous metal at a magnetic field $H_{M1}$, The Hall resistance $\rho_{xy}$, zero in the superconductor because of electron-hole symmetry, remains zero for a wide range of magnetic fields, before becoming finite at a field $H_{M2}$ well below $H_{c2}$, the superconducting critical field. This apparent electron-hole symmetric behavior may herald the appearance of what has been termed the "elusive" Bose metal (19, 20).

RESULTS

Figure 1 depicts a set of resistive transitions at increasing magnetic fields measured on amorphous TaN$_x$ and InO$_x$ films (pictured in Fig. 1A). Sample growth and characterization details are described in the Supplementary Materials and in previous studies (25, 26). For TaN$_x$, the transition to saturated resistance evolves smoothly, such that for magnetic fields above ~1 T, saturation of the resistance is apparent; the lower field transitions seem to continue at lower temperatures in an activated fashion as observed in MoGe (2). However, for InO$_x$, the transition from an activated behavior with a true superconducting state to a state with saturation of the resistance is more dramatic. Here, the resistance of the sample becomes immeasurably small below ~1 K for magnetic fields below 1.2 T ($T_c \approx 2.6$ K for this sample). In both materials, the saturation persists to high fields and resists comparables to the normal-state resistance. However, Hall effect measurements indicate a sharp boundary at $H_{M2}$ between the anomalous metallic phases with $\rho_{xx} < \rho_N$ and the metallic behavior that persists at higher fields.

Insight into the exotic nature of the anomalous metallic phase is obtained when we examine the behavior of the Hall effect at low temperatures, depicted for both TaN$_x$ and InO$_x$ films in Fig. 2. Whereas in strongly disordered materials, the Hall resistance was found to be zero below the superconductor-insulator transition crossing point at $H_c$ [realized by InO$_x$ films (27, 28)], the weakly disordered films here show $\rho_{xy} = 0$ up to a field $H_{M2} < H_{c2}$ (circled in Fig. 2). Furthermore, the Hall resistance is found to be zero (to our noise limit $\delta \rho_{xy}$ below which we cannot rule out a finite but very small $\rho_{xy}$) in a wide range of magnetic fields, $H_{M1} < H < H_{M2}$, where saturation of the longitudinal resistance is also observed. For TaN$_x$, the upper limit is $\delta \rho_{xy} \sim 3 \times 10^{-4}$ ohms, whereas for InO$_x$, the upper limit is $\delta \rho_{xy} \sim 5 \times 10^{-4}$ ohms.
Fig. 1. Electrical transport in disordered superconducting devices. (A) Micrograph and schematic diagram of InO\textsubscript{x} and TaN\textsubscript{x} Hall bar devices. (B and C) Resistive transitions for the TaN\textsubscript{x} (B) and InO\textsubscript{x} (C) films. Left: Zero-field resistivity versus temperature. Right: Resistive transitions in the indicated magnetic field plotted against inverse temperature, highlighting the saturated regime.

Fig. 2. Region of zero Hall effect. Hall resistivity versus temperature for weakly disordered TaN\textsubscript{x} (left) and InO\textsubscript{x} (right) films. The curves are offset vertically according to their temperature; the shaded region indicates where \( \rho_{xy} = 0 \) as a function of temperature and magnetic field, and an approximate location of \( H_{c2} \) is marked for each curve. Scale bars for \( \rho_{xy} \) are shown at the lower right.
To further elucidate the fact that there is a phase transition (or a sharp crossover at zero temperature) in the vortex state that appears at $H_{M1}$, we examine the nature of the vortex resistivity tensor in the entire field range below $H_{c2}$ in Fig. 3. Vortex motion should obey the scaling relation $\rho_{xy} \propto (\rho_{xx}^{-2}/H) \tan \theta_{H}$ (29), whether exhibiting flux flow, thermally assisted flux flow, or vortex glass (creep) behaviors.

Figure 3 shows the longitudinal resistance $\rho_{xx}(H)$, the Hall resistance $\rho_{xy}(H)$, $\rho_{xx}$ and $\rho_{xy}$ with a log scale, the ratio $\rho_{xx}^{-2}/\rho_{xy}$, and the Hall conductivity $\sigma_{xy}$ as a function of the magnetic field for InO$_x$ at temperatures below 1 K. (Data for TaN$_x$ are presented in the Supplementary Materials.) These curves capture all three field-tuned transitions in the films. First, the longitudinal resistance $\rho_{xx}$ shows the transition to the metallic state at $H_{M1}$ (Fig. 3A), above which the Hall resistance $\rho_{xy}$ is still zero (Fig. 3B). Above $H_{M2}$, both $\rho_{xx}$ and $\rho_{xy}$ show $\rho \sim \exp(H/H_0)$ scaling (Fig. 3C), previously associated with the metallic phase in MoGe. In addition, above $H_{M2}$, $\rho_{xx}$ and $\rho_{xy}$ obey scaling of $\rho_{xx}^{-2}/\rho_{xy} \propto H$ (Fig. 3D), indicating a state of dissipating vortex motion (29). This scaling fails just above $H_{M2}$ at the lowest temperature, where $\rho_{xx}^{-2}/\rho_{xy}$ decreases below the expected field-linear behavior. As a result, the Hall conductivity $\sigma_{xy}$ (Fig. 3E) starts to decrease with decreasing field and extrapolates to zero at $H_{M2}$, further supporting the picture of a particle-hole symmetric state. Because $\rho_{xx}$ extrapolates to a finite value at zero temperature in fields above $H_{M2}$, we identify this regime with a pure flux flow resistance. Finally, as we increase the field beyond $H_{c2}$, both $\rho_{xx}$ and $\rho_{xy}$ recover their normal-state values.

The identification of zero $\rho_{xy}$ in the anomalous metallic regime needs to be tested against the possibility that it is too low to measure.
because of the appearance of local superconducting “puddles." In particular, because the anomalous metal–superconductor system is expected to be inhomogeneous (14, 23), we may have a system of superconducting islands (for which $\sigma_{xx}^S \to \infty$ and $\sigma_{xy}^S = 0$) embedded in a metal (characterized by $\sigma_{xx}^M$ and $\sigma_{xy}^M$). If the metal percolates, then for any dilution of the system by superconducting “islands” the measured Hall conductivity satisfies $\sigma_{xy} = \sigma_{xy}^M$ (30); this behavior would persist until the superconductivity is quenched. In Fig. 3E, we plot $\sigma_{xy}^M$ (thick lines) along with $\sigma_{xy}$ calculated by inverting the resistivity tensor: $\sigma_{xy} = -\rho_{xy}/(\rho_{xx}^2 + \rho_{xy}^2)$. Above $H_c2$, $\sigma_{xy}$ shows normal-state behavior. However, just below $H_c2$ and well above $H_M2$, $\sigma_{xy}$ has departed from $\sigma_{xy}^M$, indicating that the anomalous metallic state (as well as the vortex liquid phase above it) is not a matrix of superconducting “puddles” embedded in a metal matrix.

**DISCUSSION**

Before we discuss the resulting phase diagram for these 2D disordered films, several points need to be emphasized. First, in the absence of superconducting attractive interactions, these films are expected to be weakly localized and insulating in the limit of zero temperature, although this limit is impossible to observe in finite-sized films with good metallic conduction. Second, the phases that we probe are all identified at finite magnetic fields and finite temperatures. In principle, in the presence of a finite magnetic field, there are no true finite-temperature superconducting phases in two dimensions in the presence of disorder (31), whereas in practice, the superconducting phase that we identify exhibits zero resistance. The transition to this phase, either as a function of temperature or magnetic field through $T_{KTB}$, but vortex-antivortex pairs are observed to proliferate through the system. The activated part of the resistive transition, just above saturation, fits a 2D collective vortex creep behavior. Hence, it is expected that by lowering the temperature toward $T = 0$, saturation is a consequence of a change in vortex transport, such as a transition to a dissipation-dominated quantum tunneling (3, 15). Finally, by building on recent connections between more strongly disordered films and the quantum Hall liquid-to-insulator transition (28), we here observe that the metallic region can be described as an analog to the composite Fermi liquid observed in the vicinity of half-filled Landau levels of the 2D electron gas (22).

**Fig. 4. Schematic phase diagram for a weakly disordered 2D superconductor.** In zero field, a true superconducting (SC) state with transition temperature $T_{KTB}$ is manifested by zero resistance (see main text). Increasing the magnetic field uncovers a transition to an anomalous metallic (a-Metal) phase at $H_{M1}$, a transition to a vortex flow-dominated superconductor at $H_{M2}$, and the mean field transition to the normal state at $H_c2$ (and $T = 0$ in field). Dashed lines, extracted from observed transitions in the longitudinal and/or transverse resistances, represent finite-temperature crossovers. True phase boundaries lie at $H = 0$ and in the limit of zero temperature.

**MATERIALS AND METHODS**

**Sample growth and characterization**

Disordered InO$_x$ films were grown using electron-beam deposition onto cleaned silicon substrates with silicon oxide; careful control of the sample growth resulted in amorphous, nongranular films (33). Films of TaN$_x$ were deposited using a commercial reactive sputtering tool (AJA International) onto plasma-etched silicon substrates. Film thicknesses (5 to 10 nm) were confirmed by x-ray reflectivity and transmission electron microscopy. In both materials, the films can be considered 2D with respect to superconductivity and localization effects. Film
compositions ($\kappa \approx 1.5$ for InO$_x$ and $\kappa \approx 1$ for TaN$_x$) were checked via x-ray reflectivity, diffraction, and photoemission spectroscopy; we adopted the notation of “InO$_x$” and “TaN$_x$” throughout the text as a reminder that the films are amorphous and nonstoichiometric. Film homogeneity was characterized using transmission electron microscopy and scanning electron microscopy, as well as optically; we found no evidence of inhomogeneity or granularity on any length scale to below the film thickness. Hall bar devices with a width of 100 $\mu$m and aspect ratios of either 2 or 4 were fabricated using conventional photolithography techniques, with argon ion milling to define the bar structure and electron beam–evaporated Ti/Au contacts with thicknesses of 10/100 nm.

**Measurement and data analysis**

We measured the longitudinal resistance $\rho_{xx}$ and the Hall resistance $\rho_{xy}$ using conventional four-point low-frequency ($\approx 10$ Hz) lock-in techniques; reported values are in the linear response regime. Magnetoresistance and Hall measurements were performed at both positive and negative fields; the Hall resistance was extracted from the transverse voltage by extracting the component antisymmetric in the magnetic field. Measurements on >10 samples for both materials were checked in multiple cryostats; data at temperatures below 2 K were obtained with the methods described in the section on September 15, 2017 http://advances.sciencemag.org/content/full/3/9/e1700612/DC1

**SUPPLEMENTARY MATERIALS**

Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/3/9/e1700612/DC1

Additional data—TaN$_x$

Hall conductivity in the presence of inhomogeneity

fig. S1. Transport regimes in TaN$_x$, comparable to Fig. 3.

**REFERENCES AND NOTES**

7. M. M. Rosario, H. Wang, Y. Zadorozhny, Y. Liu, Observation of a possible metallic state induced by a parallel magnetic field in superconducting Au$_{99.8}$In$_{0.2}$ samples with very low normal-state sheet resistance. J. Low Temp. Phys. 147, 623–631 (2007).

**Acknowledgments:** We acknowledge illuminating discussions with B. Spivak and S. Kivelson. Funding: Initial work was supported by the NSF (grant NSF-DMR-9508419). This work was supported by the Department of Energy (grant DE-AC02-76SF00515). Author contributions: N.P.B. and A.K. conceived and performed the experiments and wrote the manuscript. Competing interests: The authors declare that they have no competing interests. Data and materials availability: All data needed to evaluate the conclusions in the paper are present in the paper and/or the Supplementary Materials. Additional data related to this paper may be requested from the authors.

Submitted 28 February 2017
Accepted 16 August 2017
Published 15 September 2017

10.1126/sciadv.1700612

Particle-hole symmetry reveals failed superconductivity in the metallic phase of two-dimensional superconducting films
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Sci Adv 3 (9), e1700612.
DOI: 10.1126/sciadv.1700612